

Precalculus Review

Introduction to AP Calculus

Writing Two-Variable Linear Equations

Create linear equations given information about points, slope, and intercepts.

Solve problems by writing two-variable linear equations.

Reading Lesson 1.1

Composition of Functions

Evaluate the composition of functions.

Find the domain of the composition of functions.

Write an expression for the composition of functions.

Symmetry

Determine the symmetry of a function algebraically.

Determine the symmetry of a relation from a graph.

Piecewise Defined Functions

Determine the domain, range, and continuity of piecewise defined functions.

Evaluate piecewise defined functions.

Graph piecewise defined functions.

Reading Lesson 1.2

Graphing Exponential Functions

Determine the domain and range of exponential functions.

Graph exponential functions.

Identify exponential functions.

Base e

Analyze exponential and logarithmic functions in base e to determine key features of the graph.

Apply properties of logarithms and exponents to solve exponential and logarithmic equations having base e.

Determine the domain and range of exponential and logarithmic functions in base e.

Modeling with Exponential and Logarithmic Equations

Model and solve real-world problems using exponential and logarithmic functions.

Reading Lesson 1.3

Parametric Equations

Define curves parametrically.

Determine the Cartesian equation that contains a given parametric equation.

Graph parametric equations.

Reading Lesson 1.4



Function Inverses

Find the inverse of a function.

Use composition to verify that functions are inverses.

Graphing Logarithmic Functions

Determine the domain and range of logarithmic functions.

Identify and analyze the graphs of logarithmic functions.

Identify logarithmic functions.

Properties of Logarithms

Evaluate, expand, and simplify logarithmic expressions using properties of logarithms.

Reading Lesson 1.5

Radian Measure

Convert between degree and radian measure.

Use the definition of radian measure to calculate arc lengths, radii, and angle measures.

Evaluating the Six Trigonometric Functions

Evaluate the six trigonometric functions for angles in degrees or radians based on one or more given trigonometric function values.

Evaluate the six trigonometric functions for angles in degrees or radians given a point on the terminal ray.

Solving Trigonometric Equations

Analyze key features of inverse trigonometric functions from equations and graphs.

Evaluate inverse trigonometric functions over a specified domain.

Solve trigonometric equations over a specified domain.

Modeling with Periodic Functions

Model and solve real-world problems using periodic functions.

Reading Lesson 1.6

Unit Test

Analyze exponential and logarithmic functions in base e to determine key features of the graph.

Analyze key features of inverse trigonometric functions from equations and graphs.

Apply properties of logarithms and exponents to solve exponential and logarithmic equations having base e.

Define curves parametrically.

Determine the domain, range, and continuity of piecewise-defined functions.

Determine the symmetry of a function algebraically.

Evaluate the six trigonometric functions for angles in degrees or radians based on one or more given trigonometric function values.

Evaluate, expand, and simplify logarithmic expressions using properties of logarithms.

Find the domain of the composition of functions.

Model and solve real-world problems using exponential and logarithmic functions.

Model and solve real-world problems using periodic functions.

Solve trigonometric equations over a specified domain.



Limits and Continuity

Introduction to Unit 2

Rates of Change, Limits, and the Squeeze Theorem

Compare average speed to instantaneous speed.

Define the limit of a function and the properties of limits.

Determine average speed.

Determine one-sided and two-sided limits of functions.

Identify conditions under which a limit does and does not exist.

Use the squeeze theorem to indirectly find limits.

Reading Lesson 2.1

Limits Involving Infinity and Vertical and Horizontal Asymptotes

Calculate limits as x goes to positive and negative infinity.

Determine end behavior of a function using limits.

Find vertical and horizontal asymptotes using limits.

Reading Lesson 2.2

Continuous Functions and Intermediate Value Theorem

Identify intervals of continuity and discontinuity over intervals of a function.

Identify types of discontinuity, including jump, infinite, and oscillating.

Modify or extend a function to remove discontinuities.

Use properties of continuous functions to determine function continuity over algebraic combinations.

Use the intermediate value theorem to verify continuity.

Reading Lesson 2.3

Slope, Tangent Line, and Normal Line

Calculate the average rate of change of a function.

Determine the equation of the normal line to a curve at a given point.

Determine the equation of the tangent line to a curve at a given point.

Determine the slope of the tangent line at a point using limits.

Reading Lesson 2.4

Unit Test

Calculate limits as x goes to positive and negative infinity.

Calculate the average rate of change of a function.

Compare average speed to instantaneous speed.

Define the limit of a function and the properties of limits.

Determine average speed.

Determine end behavior of a function using limits.

Determine one-sided and two-sided limits of functions.



Unit Test (cont'd)

Determine the equation of the normal line to a curve at a given point.

Determine the equation of the tangent line at a given point.

Determine the slope of the tangent line at a point using limits.

Find vertical and horizontal asymptotes using limits.

Identify conditions when a limit does and does not exist.

Identify intervals of continuity and discontinuity over intervals of a function.

Identify types of discontinuity, including jump, infinite, and oscillating.

Modify or extend a function to remove discontinuities.

Use properties of continuous functions to determine function continuity after algebraic combinations.

Use the intermediate value theorem to verify continuity.

Use the sandwich theorem to find limits indirectly.

Derivatives

Introduction to Unit 3

Derivatives of Functions

Approximate the derivative of a function from a given data set.

Calculate the derivative of a function at a point.

Determine if a function is differentiable on a closed interval.

Determine the derivative of a function using the definition of a derivative.

Sketch a graph of a function when given the graph of its derivative.

Sketch a graph of the derivative of a function when given its graph.

Reading Lesson 3.1

Derivatives and Continuity

Estimate derivatives using graphs and numerical approximation.

Identify different types of non-differentiable points, including discontinuities, vertical tangents, corners, and cusps.

Reading Lesson 3.2

Differentiation Rules

Calculate instantaneous rate of change using the derivative.

Calculate second derivatives and higher-order derivatives using rules of differentiation.

Use the power rule to find derivatives.

Use the product rule to find derivatives.

Use the quotient rule to find derivatives.

Reading Lesson 3.3



Applications of Derivatives

Solve real-world problems involving rates of change using derivatives.

Use derivatives to solve problems involving motion in a straight line.

Reading Lesson 3.4

Differentiating Trigonometric Functions

Determine derivatives of trigonometric functions.

Reading Lesson 3.5

AP Multiple Choice/Free Response

Unit Test

Calculate second derivatives and higher order derivatives using rules of differentiation.

Compute the derivative of a function at a point.

Compute the derivative of a function using the definition of a derivative.

Determine if a function is differentiable on a closed interval.

Determine the derivatives of the six basic trigonometric functions using the rules of differentiation.

Estimate derivatives using graphs and numerical approximation.

Identify different types of non-differentiable points, including discontinuities, vertical tangents, corners, and cusps.

Sketch a graph of a function when given the graph of its derivative.

Sketch a graph of the derivative of a function when given a data set.

Sketch a graph of the derivative of a function when given its graph.

Solve real-world problems involving rates of change using derivatives.

Use derivatives to solve problems involving motion in a straight line.

Use the power rule to find derivatives.

Use the product rule to find derivatives.

Use the quotient rule to find derivatives.

More Derivatives

Introduction to Unit 4

Differentiating Functions Using the Chain Rule

Apply the chain rule to find the derivative of a composite function.

Use the chain rule to determine the slopes of curves defined parametrically.

Reading Lesson 4.1

Differentiating Functions Using Implicit Differentiation

Determine derivatives using implicit differentiation.

Use the power rule to find the derivative of a function raised to a rational power of x.

Reading Lesson 4.2



Differentiating Functions Containing Inverse Trigonometric Functions

Determine derivatives of inverse functions using the chain rule.

Determine derivatives of inverse trigonometric function.

Reading Lesson 4.3

Differentiating Exponential and Logarithmic Functions

Calculate derivatives of exponential functions with a base of e.

Calculate derivatives of exponential functions with a base other than e.

Calculate derivatives of logarithmic functions with a base other than e.

Calculate derivatives of natural logarithmic functions.

Reading Lesson 4.4

Unit 4 AP Practice Questions

Unit Test

Apply the chain rule to find the derivative of a composite function.

Determine derivatives of exponential functions with a base of e.

Determine derivatives of exponential functions with a base other than e.

Determine derivatives of inverse functions using the chain rule.

Determine derivatives of inverse trigonometric functions.

Determine derivatives of logarithmic functions with a base other than e.

Determine derivatives of natural logarithmic functions.

Determine derivatives using implicit differentiation.

Use the chain rule to determine the slope of curves defined parametrically.

Use the power rule to find the derivative of a function raised to a rational power of x.

Applications of Derivatives

Introduction to Unit 5

Relative and Absolute Extrema

Determine critical points of a function.

Determine if the extreme value theorem applies to a function on a specific interval.

Identify the absolute minimum and maximum values of a function.

Identify the relative minimum and maximum values of a function.

Reading Lesson 5.1

The Mean Value Theorem

Determine increasing and decreasing intervals of a function.

Use the mean value theorem to determine the value where the derivative is equal to the average rate of change.

Reading Lesson 5.2



First and Second Derivative Test

Use the first and second derivative tests to graph f(x) from f'(x).

Use the first derivative test to determine relative extrema.

Use the second derivative test to determine concavity and points of inflection.

Reading Lesson 5.3

Application Problem Solving

Solve optimization problems using derivatives.

Reading Lesson 5.4

Newton's Method, Linearization, and Differentials

Apply Newton's method to approximate zeros of a function.

Approximate the change in *f* using differentials.

Use linearization to approximate tangent lines.

Reading Lesson 5.5

Application of Implicit Differentiation

Use implicit differentiation to solve related rate problems.

Reading Lesson 5.6

Unit 5 AP Practice Questions

Unit Test

Determine critical points of a function.

Determine increasing and decreasing intervals of a function.

Identify the relative maximum and minimum values of a function.

Solve optimization problems using derivatives.

Use the extreme value theorem to determine if a function is continuous.

Use the first and second derivative test to graph f from f'.

Use the first derivative test to determine relative extrema.

Use the mean value theorem to determine the value where the derivative is equal to the average change.

Use the second derivative test to determine concavity and points of inflection.

Approximate the change in *f* using differentials.

Use implicit differentiation to solve related rate problems.

Use linearization to approximate tangent lines.

Definite Integrals

Introduction to Unit 6

Estimating with Finite Sums

Approximate a distance using area under a velocity curve.

Approximate the area under a curve by using left, right, and midpoint sums.

Solve accumulation problems by approximating the area under a curve.



Reading Lesson 6.1: Estimating with Finite Sums

Definite Integrals

Evaluate a definite integral using an area formula.

Evaluate definite integrals of functions with discontinuities.

Use definite integrals to solve problems involving accumulation.

Use integral notation to express a limit of Riemann sums.

Reading Lesson 6.2: Definite Integrals

Definite Integrals and Antiderivatives

Apply the mean value theorem to determine a point at which a function assumes its average value over a closed interval.

Calculate the area under a curve using antidifferentiation.

Solve problems using the properties of definite integrals.

Reading Lesson 6.3: Definite Integrals and Antiderivatives

Fundamental Theorem of Calculus, Parts 1 and 2

Use the first part of the fundamental theorem of calculus to solve problems.

Use the second part of the fundamental theorem of calculus to solve problems.

Reading Lesson 6.4: Fundamental Theorem of Calculus

Trapezoidal Rule

Approximate the area under a curve using the trapezoidal rule.

Compare the trapezoidal rule to other area approximations including left, right, and midpoint sums.

Reading Lesson 6.5: Trapezoidal Rule

Unit 6 AP Practice Questions

Unit Test

Apply the mean value theorem to determine a point at which a function assumes its average value over a closed interval.

Approximate a distance using area under a velocity curve.

Approximate the area under a curve by using left, right, and midpoint sums.

Approximate the area under a curve using the trapezoidal rule.

Calculate the area under a curve using antidifferentiation.

Compare the trapezoidal rule to other area approximations including left, right, and midpoint sums.

Evaluate a definite integral using an area formula.

Evaluate definite integrals of functions with discontinuities.

Solve accumulation problems by approximating the area under a curve.

Solve problems using the properties of definite integrals.

Use definite integrals to solve problems involving accumulation.

Use integral notation to express a limit of Riemann sums.

Use the first part of the fundamental theorem of calculus to solve problems.

Use the second part of the fundamental theorem of calculus to solve problems.



Mathematical Modeling Using Differential Equations

Introduction to Unit 7

Slope Fields

Use a slope field to find a graphical solution for a given differential equation.

Use initial conditions to find solutions to differential equations.

Reading Lesson 7.1: Slope Fields and Euler's Method

Antidifferentiation by Substitution

Evaluate indefinite integrals without using substitution.

Use substitution as a method of evaluating indefinite and definite integrals.

Verify an antiderivative formula.

Reading Lesson 7.2: Antidifferentiation by Substitution

Exponential Growth and Decay

Predict temperatures by using Newton's law of cooling.

Use exponential functions to model growth and decay.

Use separation of variables to solve initial value problems.

Reading Lesson 7.4: Exponential Growth and Decay

Unit 7 AP Practice Questions

Unit Test

Evaluate indefinite integrals without using substitution.

Use a slope field to find a graphical solution for a given differential equation.

Use exponential functions to model growth and decay.

Use initial conditions to find solutions to differential equations.

Use separation of variables to solve initial value problems.

Use substitution as a method of evaluating indefinite and definite integrals.

Verify an antiderivative formula.

Applications of Definite Integrals

Introduction to Unit 8

Integral as Net Change

Calculate the displacement of an object from a given velocity function.

Calculate the total distance an object travels from a given velocity function.

Express the net change of a quantity as a definite integral.

Find the net change of a quantity from a rate of change that is given in graphical or tabular form.

Find the net, or accumulated, change of a quantity from a rate of change function.

Reading Lesson 8.1: Accumulation and Net Change



Areas in the Plane

Calculate the area between two curves defined by only two functions and over a closed interval by integrating with respect to x.

Calculate the area between two curves defined by only two functions and over a closed interval by integrating with respect to y.

Use subregions to calculate the area between two curves over a closed interval.

Reading Lesson 8.2: Areas in the Plane

Volumes

Find the volume of a solid generated by revolving a line or curve around a given line.

Find the volume of a solid generated by revolving a region bounded by two or more lines or curves around a given line.

Find the volume of a solid with known cross sections.

Use a definite integral to express the volume of a solid.

Reading Lesson 8.3: Volumes

Applications from Science and Statistics

Use the definite integral to solve problems involving fluid pressure.

Use the definite integral to solve problems involving probabilities.

Use the definite integral to solve problems involving work.

Reading Lesson 8.5: Applications from Science and Statistics

L'Hôpital's Rule and Other Applications

Apply L'Hôpital's rule to evaluate the limit of an indeterminate form.

Compare the growth rates of functions.

Reading Lesson 9.2 and 9.3: L'Hôpital's Rule and Other Applications

Unit 8 AP Practice Questions

Unit Test

Apply L'Hôpital's rule to evaluate the limit of an indeterminate form.

Calculate the area between two curves defined by only two functions and over a closed interval by integrating with respect to x.

Calculate the area between two curves defined by only two functions and over a closed interval by integrating with respect to y.

Calculate the displacement of an object from a given velocity function.

Calculate the total distance an object travels from a given velocity function.

Compare the growth rates of functions.

Express the net change of a quantity as a definite integral.

Find the net change of a quantity from a rate of change that is given in graphical or tabular form.

Find the net, or accumulated, change of a quantity from a rate of change function.

Find the volume of a solid generated by revolving a line or curve around a given line.

Find the volume of a solid generated by revolving a region bounded by two or more lines or curves around a given line.

Find the volume of a solid with known cross sections.

Use a definite integral to express the volume of a solid.

Use subregions to calculate the area between two curves over a closed interval.



Review

Preparing for the Exam

Review: Limits and Continuity

Review: Derivatives

Review: Applications of Derivatives

Review: Integrals

Review: Applications of Integrals Review: Differential Equations

Practice Exam 1 - Part A

Analyze differential equations to obtain general and specific solutions.

Analyze functions defined by an integral.

Analyze functions for intervals of continuity or points of discontinuity.

Apply definite integrals to problems involving the average value of a function.

Calculate a definite integral using areas and properties of definite integrals.

Calculate antiderivatives.

Calculate derivatives.

Deduce and interpret behavior of functions using limits.

Determine higher-order derivatives.

Determine limits of functions.

Determine the applicability of important calculus theorems using continuity.

Estimate limits of functions.

Evaluate definite integrals.

Express limits symbolically using correct notation.

Express the limit of a Riemann sum in integral notation.

Identify the derivative of a function as the limit of a difference quotient.

Interpret limits expressed symbolically.

Interpret the definite integral as the limit of a Riemann sum in integral notation.

Interpret the meaning of a definite integral within a problem.

Interpret the meaning of a derivative within a problem.

Recognize antiderivatives of basic functions.

Recognize the connection between differentiability and continuity.

Solve problems involving slope of a tangent line.

Verify solutions to differential equations.



Practice Exam 1 - Part B

Apply definite integrals to problems involving areas and volume.

Apply definite integrals to problems involving motion.

Apply the Mean Value Theorem to describe the behavior of a function over an interval.

Approximate a definite integral.

Estimate derivatives.

Estimate solutions to differential equations.

Interpret, create, and solve differential equations from problems in contexts.

Solve problems involving rates of change in applied contexts.

Solve problems involving related rates, optimization, and rectilinear motion.

Solve problems involving slope of a tangent line.

Use derivatives to analyze properties of a function.

Use the definite integral to solve problems in various contexts.

Practice Exam 1 - Free Response Section

Practice Exam 2 - Part A

Analyze differential equations to obtain general and specific solutions.

Analyze functions defined by an integral.

Analyze functions for intervals of continuity or points of discontinuity.

Apply definite integrals to problems involving the average value of a function.

Calculate a definite integral using areas and properties of definite integrals.

Calculate antiderivatives.

Calculate derivatives.

Deduce and interpret behavior of functions using limits.

Determine higher-order derivatives.

Determine limits of functions.

Determine the applicability of important calculus theorems using continuity.

Estimate limits of functions.

Evaluate definite integrals.

Express limits symbolically using correct notation.

Express the limit of a Riemann sum in integral notation.

Identify the derivative of a function as the limit of a difference quotient.

Interpret limits expressed symbolically.

Interpret the definite integral as the limit of a Riemann sum in integral notation.

Interpret the meaning of a definite integral within a problem.

Interpret the meaning of a derivative within a problem.



Practice Exam 2 – Part A (cont'd)

Recognize antiderivatives of basic functions.

Recognize the connection between differentiability and continuity.

Solve problems involving slope of a tangent line.

Verify solutions to differential equations.

Practice Exam 2 - Part B

Apply definite integrals to problems involving areas and volume.

Apply definite integrals to problems involving motion.

Apply the Mean Value Theorem to describe the behavior of a function over an interval.

Approximate a definite integral.

Estimate derivatives.

Estimate solutions to differential equations.

Interpret, create, and solve differential equations from problems in contexts.

Solve problems involving rates of change in applied contexts.

Solve problems involving related rates, optimization, and rectilinear motion.

Solve problems involving slope of a tangent line.

Use derivatives to analyze properties of a function.

Use the definite integral to solve problems in various contexts.

Practice Exam 2 - Free Response Section